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Formation of charged soot aggregates by combustion and pyrolysis: charge distribution and photophoresis

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Abstract

Soot aggregates formed by propane combustion in a diffusion flame and benzene pyrolysis in a flow reactor are studied by a microscopic video system (at standard temperature and pressure) and transmission electron microscope. The radius of soot aggregates is in the range 0.1–1.0 μm . The size of primary particles in aggregates is 10–30 nm for the combustion aggregates and 40–200 nm for the pyrolysis aggregates. By video observations of aggregate movement in the electric field it is determined that soot aggregates are charged. The typical aggregate charge is a few elementary units. The soot charge distribution is roughly bipolar and symmetric. This charge distribution is governed by the Boltzmann law with the charging equivalent diameter d_E being larger than the aggregate mean mobility diameter by a factor of 1.4, 3.0 and 1.8 for soots sampled from the flame axis, region over the flame and from the flow reactor, respectively.

Photophoretic movement of soot aggregates driven by a helium–neon laser beam (3 W/cm^2) is observed by the video system. The aggregate photophoretic velocity is determined to be increasing from 15 to 160 $\mu\text{m/s}$ with the equivalent radius increasing from 0.1 to 2.9 μm . Estimations of the sun photophoretic velocity $V_{\text{Ph}}^{\text{Sun}}$ (in the Earth's atmosphere at ground level) indicate that it is about 20% of the settling velocity for the range of aggregate radii studied in this work. The velocities of soot aggregate photophoresis in the Earth thermal irradiation were estimated to be negligible with regard to the settling velocity.

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Keywords: Soot particles; Charge distributions; Photophoresis

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Nomenclature

C_C	Cunningham correction factor
D	aggregate diffusion coefficient
D_f	fractal-like dimension
d_E	charging equivalent diameter
E	electric field strength
e	elementary charge (4.8×10^{-10} units of CGSE)
F_D	drag force
F_{Ph}^{agg}	photophoretic force acting to the aggregate
F_{Ph}^{single}	photophoretic force acting to a single spherical particle of radius r
F_{Ph}^{Sun}	sun photophoretic force
$f(q)$	charge distribution function
f_1	input flow rate in the benzene pyrolysis reactor
f_2	nitrogen dilution flow rate in the benzene pyrolysis reactor
f_3	air dilution flow rate in the benzene pyrolysis reactor
g	acceleration due to gravity
I	intensity of light ($\text{erg cm}^{-2} \text{s}^{-2}$)
J_1	photophoretic asymmetry factor
k	imaginary part of refractive index
k_B	Boltzmann constant ($k_B = 1.38066 \times 10^{-23} \text{ J/K}$)
k_p	benzene pyrolysis rate constant
$Kn = \lambda/r$	Knudsen number
m	mass of gas molecules
M	aggregate mass
n_c	charge number of the aggregate
n	real part of refractive index
$q = n_c e$	aggregate charge
p_0	ambient gas pressure
r	radius of a single particle
$R \left(= \frac{1}{2} \sqrt{LW} \right)$	aggregate radius determined by transmission electron microscopy images, L and W are the length and width of the smallest rectangle enclosing the aggregate's image
R_a	equivalent projected area radius
R_m	mobility equivalent radius of aggregate
T	temperature
t	reaction time
v	aggregate velocity
v_{settl}	aggregate settling velocity
V_{Ph}^{single}	photophoretic velocity of single particle
V_{Ph}^{Sun}	sun photophoretic velocity
$[C_6H_6]$	benzene concentration at the reactor outlet
$[C_6H_6]_0$	benzene concentration at the reactor inlet

ξ	benzene decomposition degree
λ	gas mean free path
η	viscosity coefficient
χ_a	coefficient of thermal conductivity for gas
χ_i	coefficient of thermal conductivity for material of particle

1

1. Introduction

3 Soot emission to the atmosphere from vehicles, industrial machines, oil fires and others can add
4 considerably to the Earth's energy budget and climate (Colbeck, Appleby, Hardman, & Harrison,
5 1990; Bergstrom, Russell, & Hignett, 2002; Chylek et al., 1996). On the other hand, soot exhaust
6 can result in hazardous air pollution being a means for the transportation of semivolatile toxic
7 combustion products. Soot particles (or aggregates of primary particles) of size 0.01–0.1 μm can
8 penetrate and remain in the alveolar regions of the human lungs, causing local reactions, long-term
9 chronic damage, resulting in mutagenic and carcinogenic effects (Koshland, 1996).

10 Most often soot is emitted to the atmosphere as aerosol aggregates composed of small primary
11 particles (see, for example, Nyeki & Colbeck, 1995; Köylü, Mcenally, Rosner, & Pfefferle, 1997;
12 Dobbins & Subramaniasivan, 1994). The morphology of the aggregates is a crucial factor which
13 determines the transport of soot in the atmosphere, optical properties, efficiency to penetrate to
14 the lungs of human and animals, and the aggregate surface area able to adsorb harmful combustion
15 products. Soot aggregate morphology is controlled by different factors such as humidity (which leads
16 to restructuring of aggregates to compact structures (Colbeck et al., 1990)), high temperature (which
17 causes soot aggregate restructuring in the flame (di Stasio, 2001)) and electric charge on aggregates.
18 The aggregate charge can effect the morphology at the stage of cluster–cluster aggregation (Richter,
19 Sander, & Cheng, 1984; Hurd & Flower, 1988; Zhang, Sorensen, Ramer, Olivier, & Merklin, 1988;
20 Julien & Meakin, 1989; Park, Kim, & Chang, 2001), and, besides, the charge can govern the
21 aggregate restructuring resulting in transformation of chain-like structures to compact ones (Onischuk
22 et al., 2003). It is known also that the lung deposition of inhaled aerosol may be significantly
23 enhanced by the electric charges carried by particles (or aggregates of particles) (Vincent, 1985).

24 Thus, the electric charge of soot aggregates is an important parameter which affects the aggregate
25 morphology and other properties. It was shown (see, for example, Place & Weinberg, 1966; Ball
26 & Howard, 1971; Wersborg, Howard, & Williams, 1973; Onischuk et al., 2003; Burtscher, Reist,
27 & Schmidt-Ott, 1986; Roth & Hospital, 1994; Popovicheva, Persiantseva, Starik, & Loukhonitskaya,
28 2003; Sorokin, Vancassel, & Mirabel, 2003) that soot aggregates formed in combustion are charged
29 as well as flame generated inorganic aggregates (see, for example, Katzer, Weber, & Kasper, 2001).
30 The soot aggregate charge arises from bipolar ion diffusion in the reaction zone (Calcote, 1981;
31 Calcote & Gill, 1994; Burtscher et al., 1986; Rogak & Flagan 1992; Wen, Reischl, & Kasper, 1984a;
32 Alonso, Hashimoto, Kousaka, Higuchi, & Nomura, 1998; Fuchs, 1964). It seems to be evident that
33 the study of charge distribution for soot aggregates synthesized through different combustion and
pyrolysis routes is important.

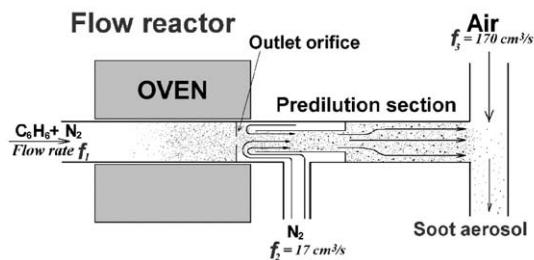


Fig. 1. Scheme of flow reactor.

1 Many particles present in the atmosphere, including soot, experience a force when exposed to
 2 visible light which causes them to migrate towards or away from the light source. This phenomenon is
 3 termed photophoresis. There is no unique opinion with regard to the role of photophoresis in vertical
 4 transport of soot in the atmosphere. The results of Kerker and Cooke (1982) suggest that the sun
 5 photophoresis force is not more than a few percent of the gravity force in the free-molecular region.
 6 However, Orr and Keng (1964) state that small particles may be very significantly influenced by the
 7 action of light in the stratosphere. Lewittes and Arnold (1982) concluded that $1 \mu\text{m}$ particles having
 8 particular dielectric and thermal properties should be levitated in the upper atmosphere by the ambient
 9 light. The recent estimations by Tehranian, Giovane, Blum, Xu, and Gustafson (2001) and Beresnev,
 10 Kovalev, and Kochneva (2003) predict the strong influence of sun photophoresis on vertical transport
 11 of soot particles at high altitudes. Besides, the numerical results of Mackowski (1989) indicate that
 12 photophoresis can be a significant transport mechanism for micrometer-sized particulates in high
 13 radiative transfer combustion environments. Thus, further theoretical and experimental studies of the
 14 role of photophoretic forces in the atmospheric particle transport, combustion and other processes
 15 are necessary.

16 This work deals with soot aggregates formed by benzene pyrolysis and propane combustion.
 17 Benzene is of interest, because the modern use of fuels with increased aromatic contents has increased
 18 particulate emissions from vehicular exhausts and industrial processes with regard to the fuels with
 19 low C/H ratio. On the other hand, propane is an important practical fuel and its combustion is
 20 characterized by the rapid decomposition into smaller intermediates C_1 – C_3 which is similar to the
 21 combustion of more complex hydrocarbon fuels (Leung, Lindstedt, & Jones, 1993). That is why
 22 propane is often used for laboratory studies of combustion processes and, particularly, soot formation
 23 mechanisms.

24 This paper is aimed at a video and transmission electron microscopy (TEM) study of charged
 25 soot aggregates formed in both benzene pyrolysis and propane combustion. Charge distributions and
 26 photophoretic movement of these aggregates are investigated.

27 2. Experimental

28 Soot was generated by both benzene pyrolysis in a flow reactor and combustion in propane/air
 29 diffusion flame. In the case of the pyrolytic route of synthesis a mixture of benzene with nitrogen
 30 is supplied to the input of flow reactor (Fig. 1) at atmospheric pressure and room temperature. The
 31 partial pressure of benzene in the input mixture is 90 Torr. The majority of experiments were carried

1 out at a temperature of 1350 K in reaction zone. Therefore, when not mentioned specially, the reactor
2 temperature should be implied as this. The input flow rate is varied in the range $f_1 = 0.25\text{--}2.5\text{ cm}^3/\text{s}$
3 at STP which corresponds to the residence time in the reaction zone $t = 0.6\text{--}6\text{ s}$. There is an orifice of
4 diameter 0.2 cm at the end of reaction zone. At the outlet of this orifice the outcoming flux is mixed
5 with a cold nitrogen supplied with flow rate of $f_2 = 17\text{ cm}^3/\text{s}$ (predilution). Downstream the soot
6 aerosol is diluted again with a flux of air $f_3 = 170\text{ cm}^3/\text{s}$ to suppress coagulation. The coagulation
7 time in the predilution section is 3 s. The soot mass concentration in the flow is determined by
8 deposition to a high efficiency Petrianov aerosol filter (Kirsch, Stechkina, & Fuchs, 1975).

9 Soot formed in a propane/air diffusion flame (Onischuk et al., 2003) was also analysed. A cylin-
10 drical burner with an inner diameter of 1 cm was fed with propane fuel (90% $\text{C}_3\text{H}_8 + 7\% \text{C}_4\text{H}_{10} + 3\%$
11 CH_4 and C_2H_6) at flow rate of $5\text{ cm}^3/\text{s}$ at STP. The length of the visible part of the flame was
12 about 22 cm. To avoid the influence of air fluctuations the flame was shielded by a co-annular
13 cylindrical iron grid of diameter 7 cm. Soot aerosol for analysis was sampled both from the flame
14 axis at different heights h above burner and from the region over the flame at $h = 27\text{ cm}$. When
15 sampling from the flame axis the soot aerosol was sucked through a nickel capillary (i.d. = 1 mm,
16 length = 6 cm) at $2\text{ cm}^3/\text{s}$ at STP at different heights above the burner. At the outlet of the capillary
17 the flux was diluted 70 times by air. Then the diluted aerosol passed through an aerosol duct to the
18 optical cell for video observations (see later the description of video system). The residence time in
19 the capillary was about 20 ms, the residence time in the aerosol duct was 10 s. When sampling from
20 the region over the flame the aerosol was sucked with the flow rate of $2.5\text{ cm}^3/\text{s}$ at STP through an
21 aerosol duct directly to the optical cell. In this case the residence time in the duct was 23 s.

22 Size and shape of soot particles were analysed by a TEM. Soot particles were sampled ther-
23 mophoretically from the flux to an electron microscopy grid covered by a polyvinylformvar film.

24 A microscopic video system was used for soot observations. Soot aerosol was injected to an
25 optical cell at atmospheric pressure and room temperature. A focused He–Ne laser beam passed
26 through the cell volume. Light scattered by aerosol particles at the angle of 90° passed through
27 a flat window to the microscope objective and then to a CCD camera connected to the video
28 system. The objective drew an image of particles presented in the illuminated volume of cell on the
29 light-sensitive CCD matrix with a magnification of 15 times. The visualization field in the optical
30 cell was near $300 \times 400\text{ }\mu\text{m}^2$. The focal depth in the object space is about $30\text{ }\mu\text{m}$. The spatial
31 resolution of the system was near $3\text{ }\mu\text{m}$ that allowed to obtain resolved images of aggregates larger
32 than $3\text{ }\mu\text{m}$. For smaller sizes, the aggregates were visible as spots. To create a homogeneous electric
33 field, two parallel electrodes were fixed in the cell. The distance between electrodes was 0.25 cm.
34 The movement of the aggregates in the electric field gave an information on the electric charge of
35 aggregates.

3. Results

3.1. Soot aggregate size and morphology

36 TEM images showed that soot was forming as aggregates composed of small primary particles
37 (Fig. 2a, b). The typical diameter of primary particles was 10–30 nm for the aggregates formed in
38 the flame and 40–200 nm for the aggregates from flow reactor.

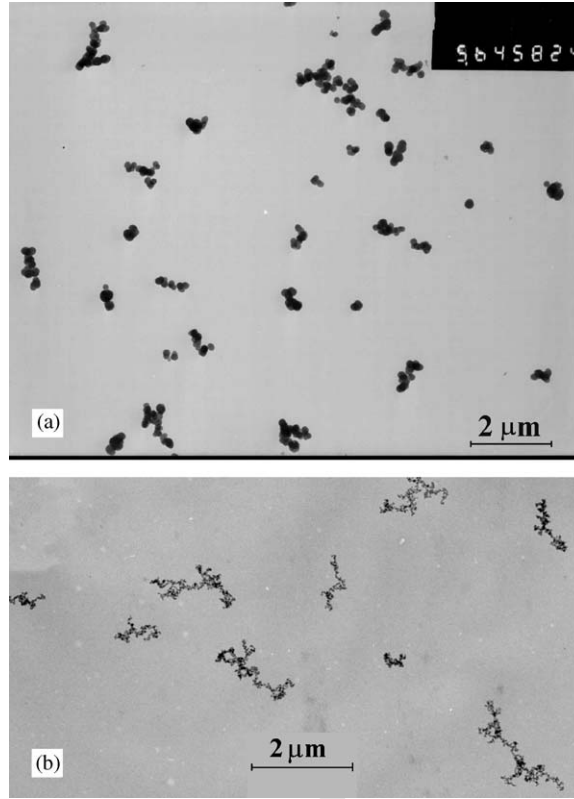


Fig. 2. TEM image of soot aggregates sampled from the flow reactor at input flow rate $f_1 = 1.4 \text{ cm}^3/\text{s}$ at SPT (a), and propane flame (from the region over the flame, height above burner $h = 27 \text{ cm}$) (b).

1 Using the TEM images the radius of aggregates was measured as

$$R = \frac{1}{2} \sqrt{LW}, \quad (1)$$

where L and W are the dimensions of the smallest rectangle enclosing the image of single particles or aggregate. Fig. 3a shows frequency distribution of aggregate radius for soot formed by benzene pyrolysis at the input flow rate $f_1 = 0.8 \text{ cm}^3/\text{s}$. Fig. 4 (circles) illustrates how the arithmetic mean radius of aggregates varies with input flow rate. One can see an increase of aggregate radius as the input flow rate increases. This increase of the aggregate radius is related to the increase of soot mass concentration in the predilution section (see Fig. 1).

We described the aggregate morphology in terms of fractal-like dimension D_f which can be determined from a power relation between the mass M of each aggregate and its radius R measured by TEM analysis (Friedlander, 2000):

$$M \propto R^{D_f}. \quad (2)$$

11 To determine D_f the values of aggregate masses were plotted as $\log M$ vs. $\log R$. To determine the aggregate mass (in arbitrary units) we measured the integral density of individual aggregate TEM

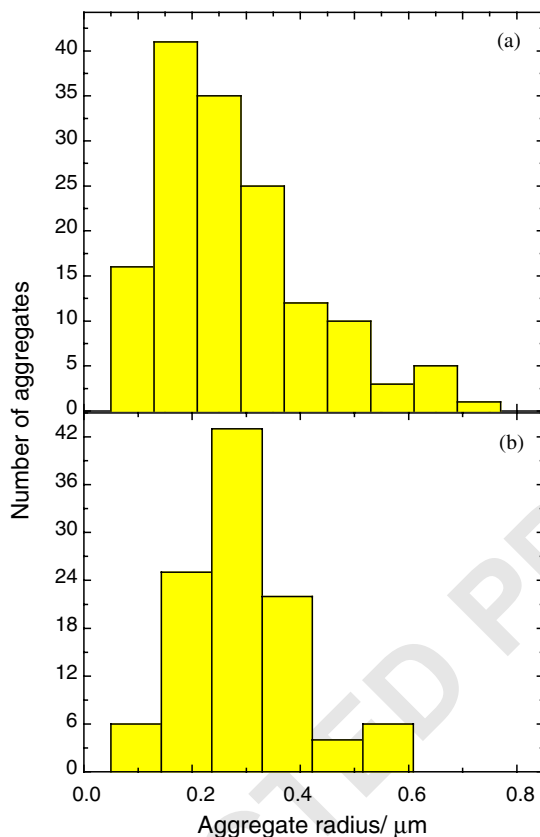


Fig. 3. Frequency distributions of aggregate radius. Soot aggregates were formed by benzene pyrolysis. Input flow rate $f_1 = 0.8 \text{ cm}^3/\text{c}$: (a) TEM data; (b) data of video observation of Brownian motion.

1 image. The procedure was as follows. The image was elaborated as a file in format “bmp”. The
 2 integral density was determined as the sum of the gray values of all the pixels which constituted
 3 the aggregate image. A correction to the background density was also done. It is assumed that the
 4 local density in the aggregate image is proportional to the local thickness of the original aggregate.
 5 Therefore, the mass of the original aggregate is considered to be proportional to the integral density
 6 of the aggregate image. This approach seems to be reasonable because it is known that even the
 7 fractal-like dimension of two-dimensional projection is approximately equal to the D_f value of the
 8 original 3D object if $D_f < 2$ (Friedlander, 2000; Rogak, Baltensperger, & Flagan, 1991). In case
 9 of soot formed by benzene pyrolysis we found that the fractal dimension does not depend on the
 10 input flow rate, being equal to $(D_f=)1.8$. Fig. 5 gives an example of $\log M$ vs. $\log R$. The fractal
 11 dimension for aggregates sampled from the region over the flame was also $(D_f=)1.8$.

12 Fig. 6 shows fraction of carbon from the initial benzene converted to soot which was determined
 13 as the ratio of soot mass concentration at the reactor outlet orifice to the mass concentration of
 14 carbon in benzene at the input. As mentioned above the majority of the results was obtained for
 15 the reactor temperature equal to 1350 K. Therefore it is interesting to compare the benzene to soot

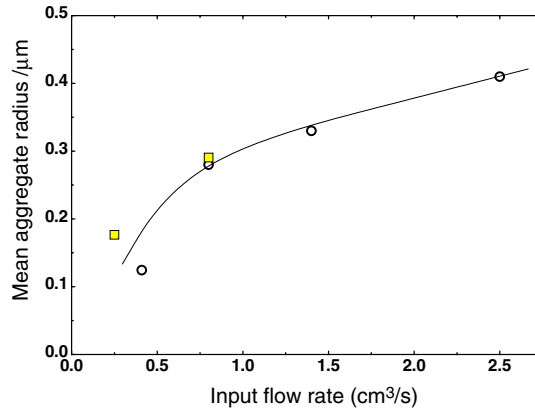


Fig. 4. Arithmetic mean radius of soot aggregates vs. input flow rate. Circles—TEM data; squares—data from the video observations of the aggregate Brownian motion. Soot aggregates were formed by benzene pyrolysis. Line is smooth fit through data.

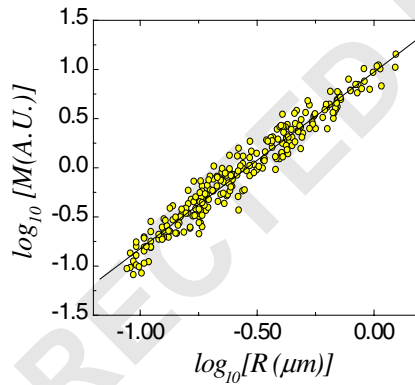


Fig. 5. Soot aggregate mass vs. radius. TEM data. Soot was formed by benzene pyrolysis at input flow rate $f_1 = 2.5 \text{ cm}^3/\text{s}$. Solid line corresponds to fractal-like dimension $D_f = 1.8$.

1 conversion with the benzene decomposition degree ξ for this temperature:

$$\xi = 1 - [\text{C}_6\text{H}_6]/[\text{C}_6\text{H}_6]_0, \quad (3)$$

3 where $[\text{C}_6\text{H}_6]$ and $[\text{C}_6\text{H}_6]_0$ are benzene concentrations at the outlet orifice and inlet of reactor, re-
 5 spectively. For the input flow rate $f_1 = 0.67 \text{ cm}^3/\text{s}$ (corresponding to Fig. 6) we have the reaction
 7 time determined from the reactor temperature profile as $t = 2.3 \text{ s}$. The effective first-order rate con-
 stant k_p of benzene pyrolysis was determined experimentally by Laskin and Lifshitz (1996) for a
 temperature $T = 1350 \text{ K}$ as equal to $k_p = 0.4 \text{ s}^{-1}$. Thus, we can estimate the benzene decomposition
 degree:

$$\xi = 1 - \exp(-k_p t) = 0.6, \quad (4)$$

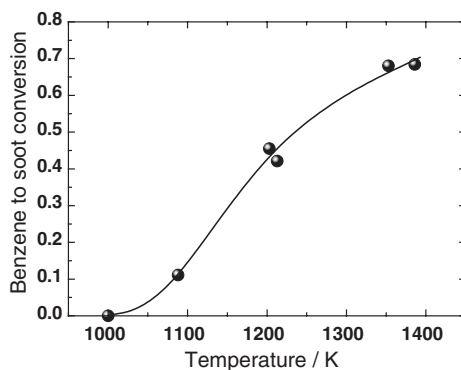


Fig. 6. Fraction of carbon from the initial benzene converted to soot vs. reactor temperature. Input flow rate $f_1=0.67 \text{ cm}^3/\text{s}$. Conversion was estimated as ratio of soot mass concentration at the outlet of reactor to the input mass concentration of carbon to be a constituent of benzene. Line is smooth fit through data.

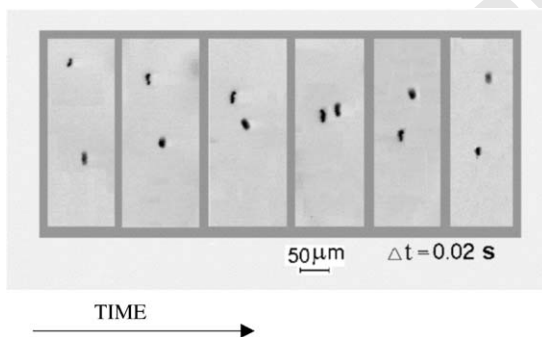


Fig. 7. A sequence of frames demonstrating movement of two charged aggregates in the electric field of 360 V/cm. The aggregates were formed in the benzene flow reactor.

- 1 which is equal to the benzene to soot conversion (Fig. 6) within the accuracy of 10%. In other
 2 words, the comparison of these estimation results with the experimentally measured benzene to soot
 3 conversion shows that the majority of decomposed benzene has converted to soot particles.

3.2. Video observations of soot aggregates

- 5 Movement of soot aggregates in the optical cell under a homogeneous electric field applied with
 6 a strength of 360 V/cm was studied using a video system. Fig. 7 gives an example of movement
 7 of two aggregates in the electric field. One can see that one of two aggregates moves downwards
 8 (negative charge), while the other aggregate moves upwards (positive charge). We estimated the
 9 aggregate net charge from the balance between the Coulomb force and the drag force F_D :

$$n_c e E = F_D, \quad (5)$$

1 where n_c is the number of the elementary charges on the aggregate, e the elementary charge (4.8×10^{-10} units of CGSE) and E the electric field strength. The drag force

$$F_D = \frac{6\pi v \eta R_m}{C_C}, \quad (6)$$

3 where η is the viscosity coefficient for air, v is the aggregate velocity, R_m is the mobility equivalent radius, C_C is Cunningham correction factor given (see, for example, Reist, 1993):

$$C_C = 1 + \frac{\lambda}{R_m} \left[A + Q \exp\left(-\frac{bR_m}{\lambda}\right) \right], \quad (7)$$

5 where $A = 1.26$, $Q = 0.40$, $b = 1.10$ and λ is the gas mean free path.

Thus, the charge of each aggregate was determined using Eqs. (5) and (6). The crucial point
7 in these estimations was determination of R_m . Two different approaches were applied. In the first approach, the mobility equivalent radius of each aggregate was derived from the observation of its
9 Brownian motion without an electric field. The aggregate diffusion coefficient D was determined from the Einstein equation:

$$\overline{(\Delta x)^2} = 2D\tau, \quad (8)$$

$$\overline{(\Delta x)^2} = \frac{\Delta x_1^2 + \Delta x_2^2 + \dots + \Delta x_N^2}{N},$$

11 where $\Delta x_1, \Delta x_2, \dots, \Delta x_N$ are successive displacements of the aggregate along the horizontal x -axis over time interval $\tau = 0.8$ s. Then the equivalent mobility radius was derived from the expression
13 for the diffusion coefficient:

$$D = \frac{k_B T C_C}{6\pi R_m \eta}, \quad (9)$$

where k_B is the Boltzmann constant and T is temperature. After recording the aggregate Brownian
15 motion the electric field was switched on to measure the velocity of aggregate movement due to an electric force. This approach resulted in a charge distribution for the aggregates as presented in
17 Fig. 8a. Fig. 3b demonstrates the frequency distribution of equivalent mobility radius determined by video observation of aggregate Brownian motion for the input flow rate $f_1 = 0.8$ cm³/s. There is
19 reasonable agreement between the radius distribution histograms determined by video observation and TEM image analysis (Fig. 3a) for this flow rate $f_1 = 0.8$ cm³/s. Fig. 4 compares TEM and
21 video data for the mean aggregate radius vs. input flow rate. The video observation overestimates the mean aggregate radius at $f_1 = 0.25$ cm³/s with regard to the TEM data. The reason for this
23 overestimation is fact that sensitivity limit of the video system approximately equal to ~ 0.1 μ m. At $f_1 = 0.8$ cm³/s there is satisfactory agreement between video and TEM data. Therefore, we assume
25 that the video system gives reasonable values of the mean mobility radius at $f_1 > 0.5$ cm³/s. In the second approach the same average radius was used to characterize each aggregate recorded
27 by the video system. This average R was determined by elaboration of TEM images. Fig. 8b shows the frequency distribution of aggregate charge for this way of data treatment. One can see a
29 good agreement between the two histograms obtained from TEM image elaboration (Fig. 8b) and video observations of Brownian motion (Fig. 8a) indicating the validity of both ways of aggregate
31 charge distribution measurement. Figs. 8a, b show that there is approximately a symmetric bipolar charge distribution of soot aggregates. The typical aggregate net charge is a few elementary units.

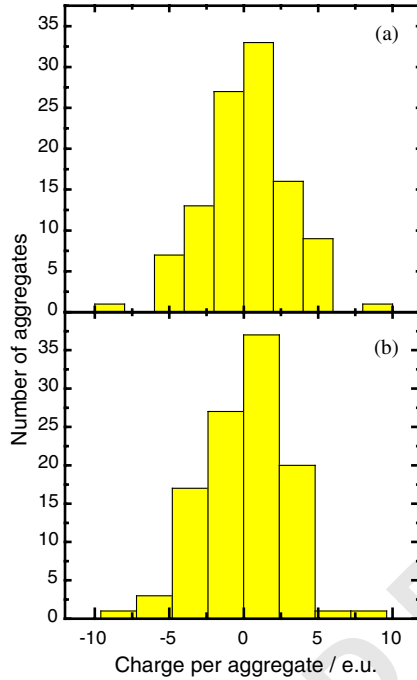


Fig. 8. Frequency distribution of aggregate charge determined by video observations. Soot was formed by benzene pyrolysis at input flow rate $f_1 = 0.8 \text{ cm}^3/\text{c}$. When estimating charge the aggregate radius was determined: (a) for each aggregate by video registration of Brownian motion and (b) by elaboration of TEM data (the same average radius was used for each aggregate).

- 1 Fig. 9 presents a scattering plot in coordinates aggregate charge–mobility radius. One can see that
 2 the greater the aggregate radius the wider the charge distribution.
- 3 Video observations showed that soot aggregates illuminated by the light of He–Ne laser moved
 4 in the direction of the beam due to photophoresis. For each aggregate observed by the video system
 5 we determined both photophoretic velocity (at the power of light beam of $3 \text{ W}/\text{cm}^2$) and equivalent
 6 radius (by Brownian motion for small aggregates or settling velocity for large ones). We found that
 7 the photophoretic velocity increased with the equivalent radius. To demonstrate the dependence of
 8 photophoretic velocity on equivalent radius we divided the experimental points into several groups,
 9 uniting the points of neighbouring radii in one group and averaging photophoretic velocities and
 10 equivalent radii in each group. Fig. 10a demonstrates this dependence of photophoretic velocity on
 11 radius. It is worth to say separately about the procedure of equivalent radius determination from the
 12 settling velocity. It was possible to observe both random Brownian motion (which gave mobility
 13 radius R_m) and settling motion for relatively small aggregates. For these aggregates, we can estimate
 14 the mass from the balance between drag force and gravity force,

$$\frac{6\pi v_{\text{settl}} \eta R_m}{C_C} = Mg, \quad (10)$$

- 15 where g is the acceleration due to gravity and v_{settl} is the settling velocity. Assuming the aggregate
 fractal dimension $D_f = 1.8$ (see Fig. 5), we can estimate equivalent mobility radius from the settling

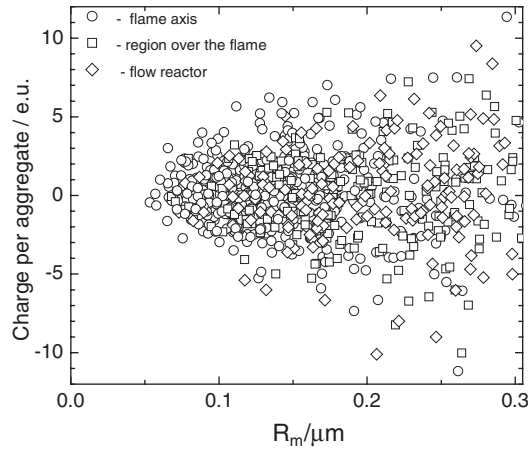


Fig. 9. Scattering graph in coordinates mobility radius—net aggregate charge. Mobility radius for each aggregate was determined by the video observation of Brownian motion. Points for soot formed by benzene pyrolysis (at the input flow rates $f_1 = 0.25$ and $0.8 \text{ cm}^3/\text{s}$) and propane combustion sampled from the flame axis (at height above burner $h = 5.5, 7.8, 10.0$ and 13.3 cm) and from the region over the flame at $h = 27 \text{ cm}$ are put in the same graph.

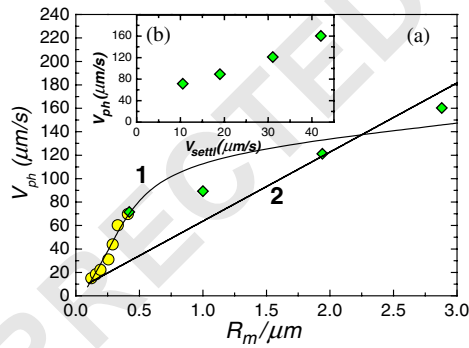


Fig. 10. (a) Aggregate photophoretic velocity vs. mobility equivalent radius of aggregates. R_m was determined by Brownian (circles) and settling motion (diamonds). (b) shows photophoretic velocity vs. settling velocity. Solid lines are estimations of aggregate photophoretic velocity: 1—Eq. (14) (single particle approximation); 2—Eq. (18) (ensemble of primary particles approximation).

1 velocity of larger aggregates (for which the Brownian movement is negligible) solving Eq. (10) with

$$M = M_0 \left(\frac{R_m}{R_m^0} \right)^{D_f}, \quad (11)$$

where R_m^0 and M_0 are mobility radius and mass of relatively small aggregate determined via obser-
 3 vation of Brownian motion and gravitational settling, respectively; M is the mass of large aggregate
 5 and R_m is mobility radius of large aggregate. The diamond points in Fig. 10a are calculated via Eqs.
 (10) and (11).

4. Discussion

4.1. Steady-state charge distribution

Aerosol particles in a bipolar ion atmosphere come to a steady-state condition. For particles larger than $0.05 \mu\text{m}$ the distribution of charges at the steady-state condition corresponds to the dynamic electrical equilibrium described by the Boltzmann law (see, for example, Hussin, Scheibel, Becker, & Porstendorfer, 1983; Liu & Pui, 1974; Wen, Reischl, & Kasper, 1984a, b; Fuchs, 1964):

$$f(q) = \frac{1}{\sum} \exp\left(-\frac{(q)^2}{d_E k_B T}\right), \quad (12)$$

$$\sum = \sum_{-\infty}^{\infty} \exp\left(-\frac{(q)^2}{d_E k_B T}\right), \quad (13)$$

where $f(q)$ is the fraction of particles which have the charge q , k_B is Boltzmann constant, T is temperature and d_E is the charging equivalent diameter. It was shown by Rogak et al. (1991) and Wen et al. (1984b) that the steady-state charging equivalent diameter for aggregates in bipolar ionic atmosphere is approximately equal to the aggregate mobility diameter.

Fig. 9 shows a scattering plot in coordinates aggregate charge–equivalent mobility radius for the soot aggregates of three kinds: sampled from the flame axis, from the region over the flame and from the flow reactor. For each kind of aggregates it is possible to select a narrow range of radius in this charge–radius diagram. In this case, we have the charge distribution for the selected range of radius. Fig. 11 demonstrates a charge distribution for soot aggregates sampled from the axis of flame with the aggregate diameter being in the range $0.20\text{--}0.25 \mu\text{m}$. This charge distribution can be fitted by the Gaussian function (12) for room temperature and $d_E = 0.35 \mu\text{m}$. This charging equivalent diameter d_E exceeds the average mobility diameter $d_m = 0.23 \mu\text{m}$. In other words, the charge distribution for these soot aggregates is wider than equilibrium being intermediate between flame temperature and room temperature equilibrium. Fig. 12 shows d_E versus d_m for soot aggregates generated in different conditions demonstrating that the charge distributions for all the three types

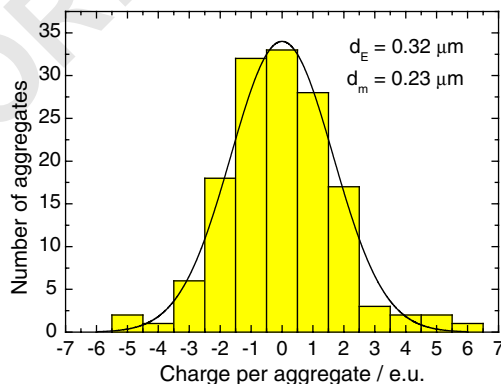


Fig. 11. Frequency distribution of aggregate net charge. The range of aggregate mobility diameter is $0.20\text{--}0.25 \mu\text{m}$. Aerosol was sampled from the flame axis. Solid line is governed by the Boltzmann equation (12) with a charging equivalent diameter $d_E = 0.32 \mu\text{m}$. Mean arithmetic mobility diameter is $0.23 \mu\text{m}$.

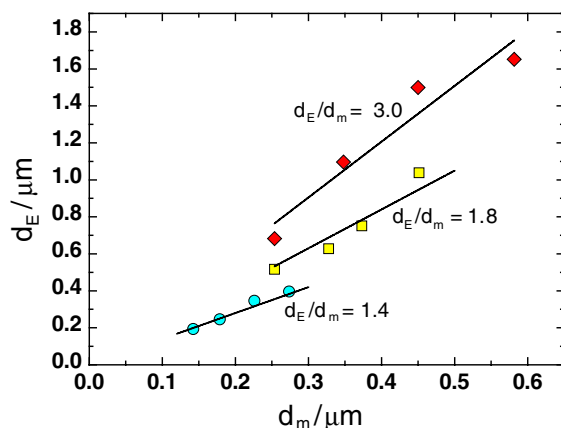


Fig. 12. Charging equivalent diameter d_E versus mobility equivalent diameter d_m for the data presented in Fig. 9. Soot was sampled from the flame axis (circles), region over the flame (diamond), and from the flow reactor (squares). Solid lines correspond to linear functions $d_E = 3.0d_m$; $d_E = 1.8d_m$; $d_E = 1.4d_m$.

1 of soot aggregates are wider than equilibrium distributions. Thus, we can conclude that there is an
 2 over-equilibrium charge distribution of soot aggregates sampled both from the flame and from the
 3 flow reactor. It is appropriate to mention that Burtcher et al. (1986) have also registered aerosol
 4 particle charge above equilibrium at room temperature for soot formed by open fires of hydrocarbons.

5 Let us discuss now some details of the over-equilibrium charge spectrum formation. Combustion
 6 and pyrolysis of hydrocarbons are characterized by a high ion concentration. Thus, the ion con-
 7 centration is 10^8 – 10^{11} cm^{-3} in the flame (Calcote, 1981; Calcote & Gill, 1994; Lewis & Von Elbe,
 8 1961) and up to 10^{15} cm^{-3} in thermal decomposition processes (Calcote, 1981). Simple estimations
 9 of charging kinetics by the collision theory show that the charge distribution on soot particles in
 10 the flame is equilibrium. When increasing distance from the reaction zone both temperature and
 11 ion concentration drops down. Therefore, the soot charge distribution becomes wider than the equi-
 12 librium distribution for this decreased temperature. The subsequent coagulation of soot aerosol is
 13 characterized by two opposite tendencies. One tendency is charge spectrum broadening due to ran-
 14 dom coagulation, the other one is aggregate charge limitation due to Coulomb interaction between
 15 colliding aggregates. It is evident that at the room temperature the second tendency of charge limi-
 16 tation due to Coulomb interaction is predominant resulting in more narrow charge spectrum than the
 17 flame temperature equilibrium distribution. On the other hand, this resulting spectrum is still wider
 18 than the room temperature equilibrium distribution.

19 4.2. Photophoresis

20 Fig. 10 demonstrates the photophoretic velocity of aggregates vs. aggregate mobility radius. One
 21 can see a monotonic increase of photophoretic velocity with equivalent mobility radius. To explain
 22 this monotonic increase we estimated the photophoretic velocity as function of aggregate radius. Two
 23 approaches were applied. In the first approach, we considered the aggregate as a single particle. In
 the case of a single spherical particle of radius r the photophoretic velocity can be estimated via the

1 expression (Beresnev et al., 2003)

$$V_{\text{Ph}}^{\text{single}} = -\frac{\pi}{2(8 + \pi)} \frac{IJ_1}{p_0} \frac{\psi_1}{\psi_3(1 + (\chi_i/\chi_a)\psi_2)}, \quad (14)$$

where ψ_1 , ψ_2 and ψ_3 are functions dependent only on Kn number ($Kn = \lambda/r$):

$$\begin{aligned} \psi_1 &= \frac{Kn}{Kn + \frac{5\pi}{18}} \left(1 + \frac{2\pi^{0.5}Kn}{5Kn^2 + \pi^{0.5}Kn + \pi/4} \right), \\ \psi_2 &= \left(0.5 + \frac{15}{4}Kn \right) \left(1 - \frac{1.21\pi^{0.5}Kn}{100Kn^2 + \pi/4} \right), \\ \psi_3 &= \frac{Kn}{Kn + 0.619} \left(1 + \frac{0.31Kn}{Kn^2 + 1.152Kn + 0.785} \right), \end{aligned} \quad (15)$$

3 p_0 is the ambient gas pressure (equal to atmospheric pressure 1.01×10^6 dyne/cm²), I the intensity
 5 of light (erg cm⁻² s⁻²), J_1 the so-called photophoretic asymmetry factor depending on the particle
 7 radius and illuminating light wavelength, λ is mean free pass for gas molecules, χ_a and χ_i are
 coefficients of thermal conductivity for gas ($\chi_a = 2.4 \times 10^3$ erg/(cm s K)) and material of particle,

9 In the second case, we considered the aggregate as an ensemble of primary particles. The pho-
 tophoretic force $F_{\text{Ph}}^{\text{agg}}$ acting to an aggregate was assumed to be equal to the sum of forces acting on
 11 primary particles. The force acting on a primary particle of radius r can be estimated via expression
 (Chernyak & Beresnev, 1993)

$$F_{\text{Ph}}^{\text{single}} = -\frac{\pi}{3} r^2 I J_1 \left(\frac{\pi m}{2k_B T} \right)^{0.5} \frac{\psi_1}{1 + (\chi_i/\chi_a)\psi_2}. \quad (16)$$

13 We can estimate the equivalent number of illuminated primary particles in the aggregate as R_a/r^2 ,
 where R_a is the radius of spherical particle with projected area equal to the projected area of
 aggregate. Thus, the aggregate photophoretic force is given by

$$F_{\text{Ph}}^{\text{agg}} = F_{\text{Ph}}^{\text{single}} (R_a/r)^2. \quad (17)$$

15 It was shown by Rogak et al. (1993) that the equivalent mobility radius R_m is approximately equal
 to the mean projected area radius R_a . Therefore, from Eqs. (16), (17) we estimate:

$$F_{\text{Ph}}^{\text{agg}} = -\frac{\pi}{3} I J_1 \left(\frac{\pi m}{2k_B T} \right)^{0.5} R_m^2 \frac{\psi_1}{1 + (\chi_i/\chi_a)\psi_2}. \quad (18)$$

17 The photophoretic velocity can be determined from the balance between the photophoretic force and
 drag force (6).

19 To estimate photophoretic velocity we need J_1 . This asymmetry factor is calculated by Beresnev
 et al. (2003) for different values of real (n) and imaginary (k) parts of the soot refractive index and
 21 different values of the wavelength. It is known (see, for example, Chang & Charalampopoulos, 1990;
 Brewster, 1992) that in the range of wavelength 0.5–1.0 μm the real and imaginary parts of refractive
 23 index are most often in the ranges $1.7 < n < 2.0$ and $0.5 < k < 0.8$ for soot. Using the values of

1 J_1 from Beresnev et al. (2003) we estimated the aggregate photophoretic velocity for both single
2 particle approximation and ensemble of primary particles approximation. Fig. 10a (curves 1 and 2)
3 demonstrates the calculation results for $n = 1.95$ and $k = 0.8$. Both curves 1 and 2 (corresponding
4 to the single particle and ensemble of particles approximations, respectively) were calculated for the
5 thermal conductivity coefficient of soot particles $\chi_i = 4.3 \times 10^5$ erg/(cm s K). One can see that both
6 curves 1 and 2 demonstrate the increase of photophoretic velocity with aggregate equivalent radius.
7 For comparison, we calculated also photophoretic velocity for $n = 1.95$ and $k = 0.5$ (not shown in
8 Fig. 10). These calculations gave $\chi_i = 3.6 \times 10^5$ erg/(cm s K) for the single particle approximation
9 and $\chi_i = 2.0 \times 10^5$ erg/(cm s K) for the ensemble of particles approximation. The curves determined
10 for these last values of the real and imaginary parts of refractive index were similar to the curves
11 1 and 2.

12 It is natural to expect that the estimated thermal conductivity coefficient for soot particles $\chi_i =$
13 $(2-4) \times 10^5$ erg/(cm s K) lies between these coefficients for polyaromatic hydrocarbons and graphite
14 which can be considered as soot precursors and the latest product in the soot formation process,
15 respectively. Indeed, the thermal conductivity coefficients for naphthalene and graphite are 3.8×10^4
16 and $\sim 1 \times 10^7$ erg/(cm s K), respectively. Thus, one can see that soot thermal conductivity coefficient
17 determined from estimations lies between these values for naphthalene and graphite in agreement
18 with our previous assumption.

19 It seems interesting to compare the measured aggregate settling velocity with possible sun pho-
20 toporetic velocity for these aggregates in the atmosphere at ground level. The sun constant is $1.368 \times$
21 10^6 erg/(cm² s) which is about 20 times less than our laser beam irradiation (3×10^7 erg/cm² s).
22 Thus, we can expect that the sun photophoretic velocity $V_{\text{Ph}}^{\text{Sun}}$ will be about 20 times less than the
23 laser photophoresis values we measured in the laboratory. Therefore, from Fig. 10b we can see that
24 $V_{\text{Ph}}^{\text{Sun}}$ is about 20% of gravitational settling velocities.

25 Beresnev et al. (2003) have demonstrated by theoretical estimations that there can be a situation
26 of soot particle levitation due to thermal irradiation of the Earth. These authors have shown that the
27 upward photophoretic force is higher than the gravity force for soot particles of size about 1.5 μm .
28 Therefore, we estimated the possible photophoretic contribution from thermal irradiation of the Earth
29 to the vertical transport of our soot aggregates in the atmosphere. The intensity of this irradiation
30 is about 4×10^5 erg/(cm² s) near the Earth's surface during the summer time (Anderson et al.,
31 1986) which is 75 times less than our laser beam irradiation. The asymmetry factor J_1 for thermal
32 irradiation of the Earth (the wavelength is $\sim 10 \mu\text{m}$) is about 6 times less than for He-Ne laser
33 wavelength. Thus, based upon the data presented in Fig. 10b, we estimate the photophoretic velocity
34 from the Earth irradiation to be about 1% of the settling velocity for the soot aggregates studied in
35 this paper.

5. Conclusions

37 By means of the video observation, charge distributions of soot aggregates synthesized by propane
38 combustion and benzene pyrolysis were determined. The charge distribution of soot aggregates is
39 above equilibrium being larger than room temperature equilibrium by a factor of 1.4, 3.0 and 1.8 for
40 soot sampled from the flame axis, region over the flame and from the flow reactor,
41 respectively.

1 Measurements of the aggregate photophoretic velocity as a function of equivalent mobility radius
 2 were done for soot aggregates formed by benzene pyrolysis. The aggregate photophoretic velocity
 3 was found to be increasing from 15 to 160 $\mu\text{m/s}$ with the equivalent radius increasing from 0.1
 4 to 2.9 μm . Estimations of sun photophoretic velocities $V_{\text{ph}}^{\text{Sun}}$ (in the Earth's atmosphere at ground
 5 level) were performed in comparison with the aggregate settling velocity. These estimations testified
 6 that $V_{\text{ph}}^{\text{Sun}}$ is about 20% of settling velocity for the range of aggregate radii studied in this work.
 7 The Earth radiation photophoresis velocity was estimated to be negligible with regard to the settling
 velocity of soot aggregates.

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